

CWI

PNA1



Algorithms, Combinatorics and Optimization

Current composition of the group

Senior researchers:

Krzysztof Apt

Bert Gerards

Monique Laurent

Guido Schaefer

Lex Schrijver

also professors at

U. Amsterdam

U. Maastricht

U. Tilburg

VU Amsterdam

U. Amsterdam

Part-time: Jan Draisma

Frank Vallentin

TU Eindhoven

TU Delft

Five postdocs & five PhD students

Guest researchers: Aharon Ben-Tal (Technion),
Vincent Conitzer (Duke), Amy Greenwald (Brown)

2005

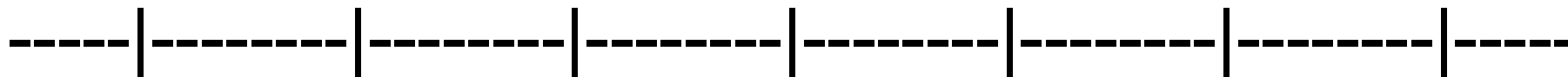
2006

2007

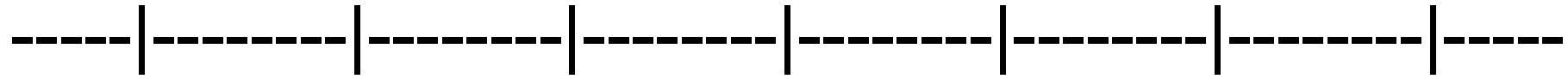
2008

2009

2010

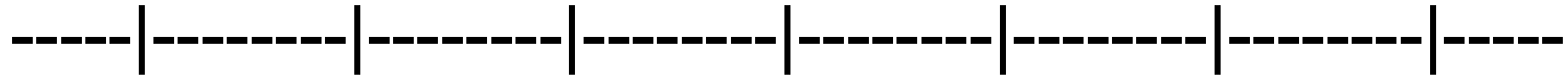


2005 2006 2007 2008 2009 2010



constraint
programming

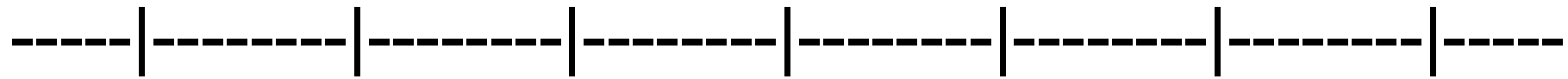
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constraint programming

integer programming

2005 2006 2007 2008 2009 2010

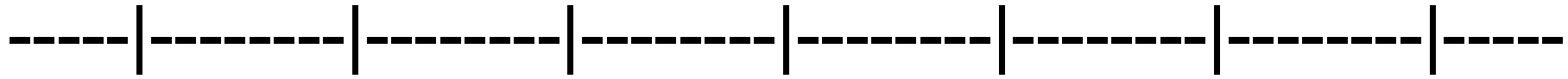


constraint programming

integer programming

combinatorial biology

2005 2006 2007 2008 2009 2010



constraint programming

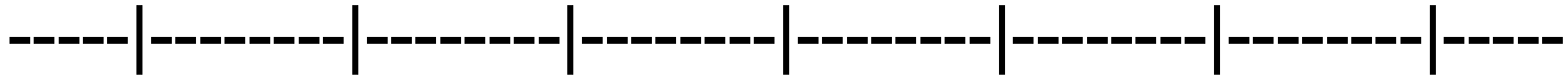
integer programming

combinatorial biology

life sciences



2005 2006 2007 2008 2009 2010



constraint programming

integer programming

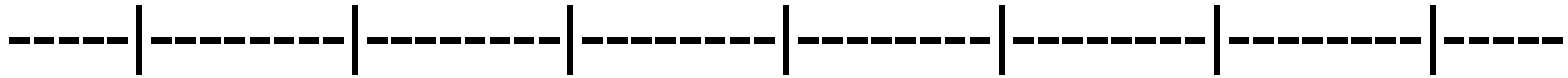
combinatorial biology

life sciences

algebraic and semidefinite programming



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constraint programming

integer programming

combinatorial biology

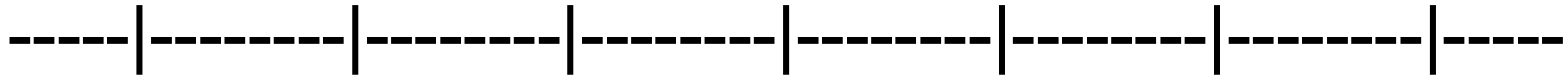
life sciences



algebraic and semidefinite programming

graph partition functions

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integer programming

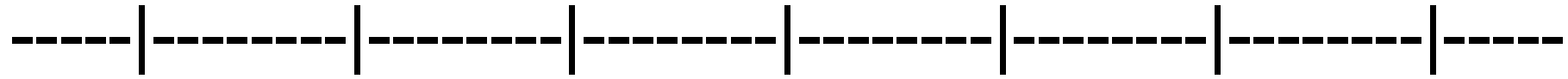
combinatorial biology → life sciences

algebraic and semidefinite programming

graph partition functions

algorithmic game theory

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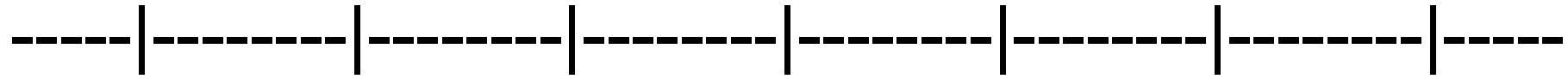
graph partition functions

algorithmic game theory

random geometric graphs



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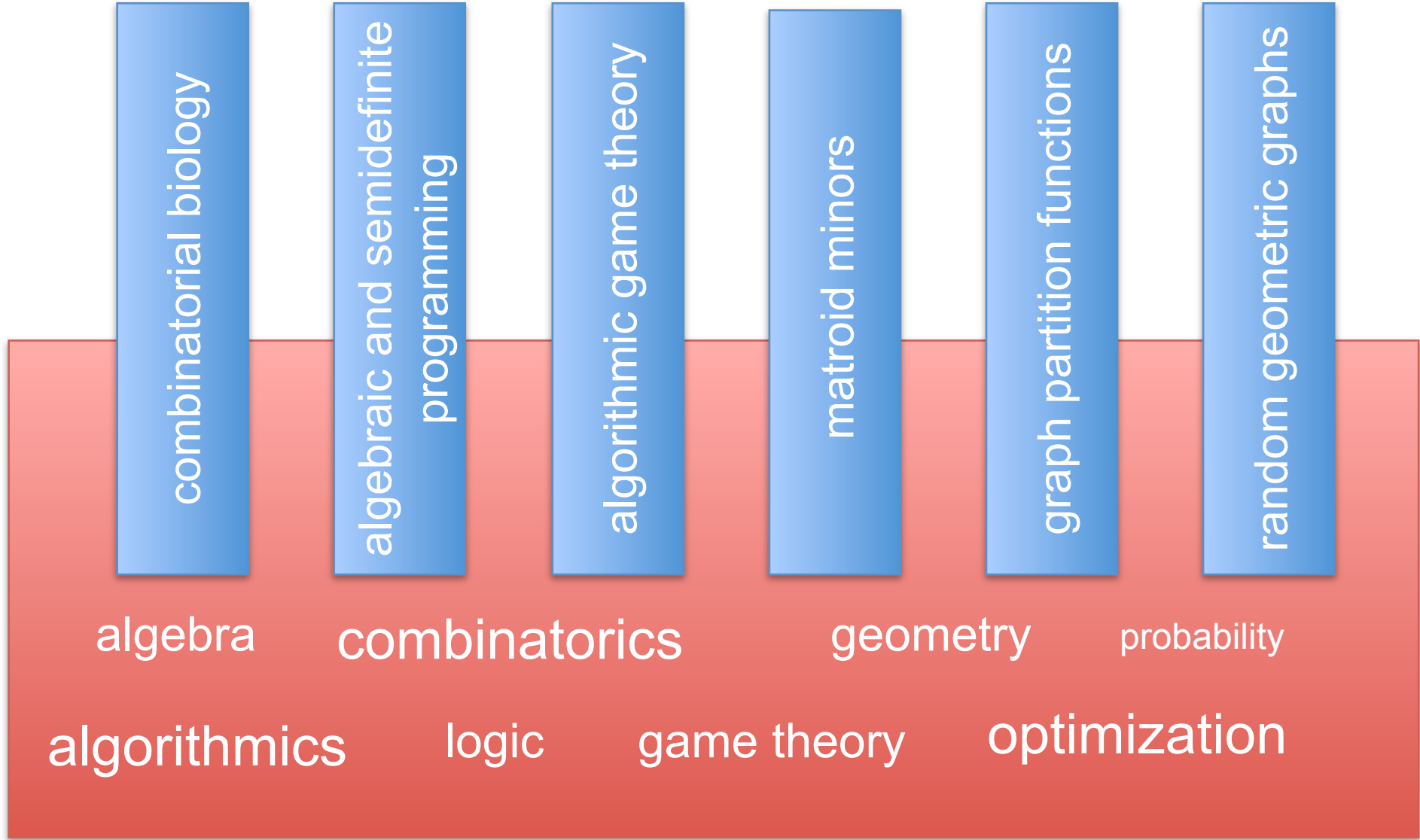
graph partition functions

algorithmic game theory

random geometric graphs

matroid minors





combinatorial biology

algebraic and semidefinite
programming

algorithmic game theory

matroid minors

graph partition functions

random geometric graphs

algebra

combinatorics

geometry

probability

algorithmics

logic

game theory

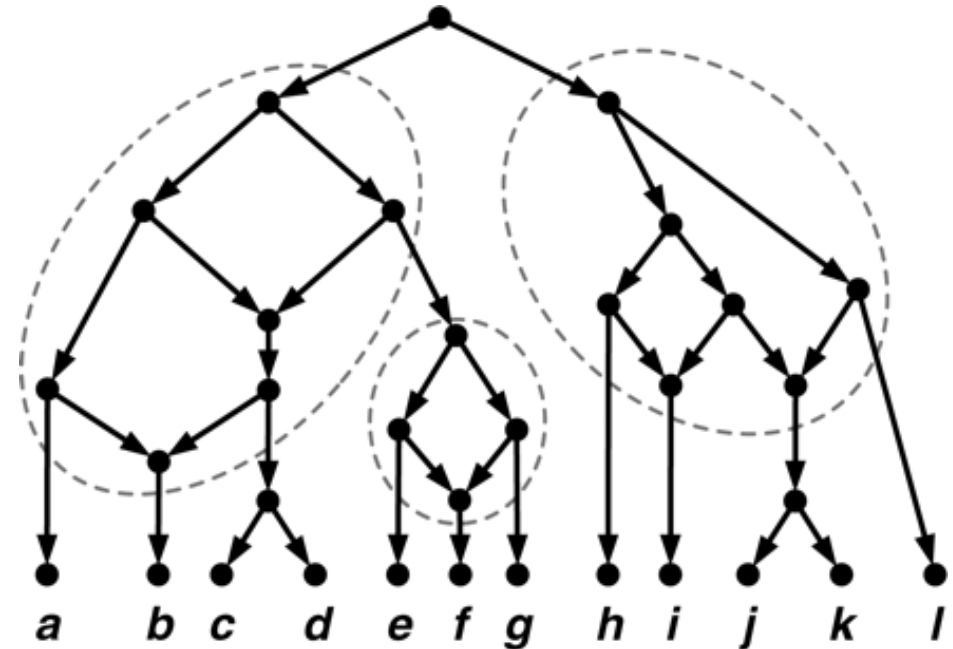
optimization

Combinatorial biology

Phylogenetic networks

- *Efficient algorithms for 2-level networks*
- *Optimal worst-case approximations*

2-level network



Metabolic networks



Joint project with MAS3 / MAC4



MAC4 [Life Sciences] since 2009

Algebraic and semidefinite programming

New area, combining tools from:

- real algebraic geometry & moment theory
- invariant theory (exploit symmetry)
- harmonic analysis
- semidefinite programming

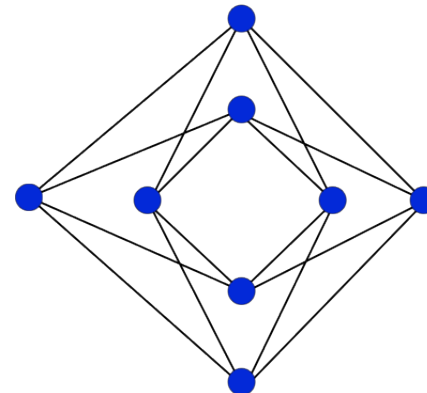
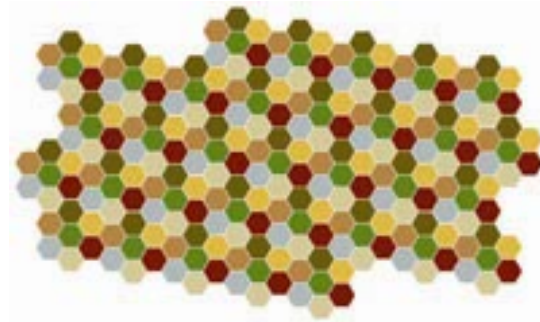
Algebraic and semidefinite programming

Highlight results

Better bounds for:

- Codes
- Graph coloring
- Crossing numbers
- Kissing numbers

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Algebraic and semidefinite programming

Future directions

- Higher order SDP relaxations
- Mixing numeric and symbolic algorithms
- Linking classical and quantum computing: Grothendieck inequalities, noncommutative polynomials,...



Joint project with PNA6

[Algorithms and Complexity]

Graph partition functions

in the spin model

$$f(G) = \sum_{\substack{\varphi: V(G) \rightarrow [k] \\ \text{vertex coloring}}} \prod_{uv \in E(G)} A_{\varphi(u), \varphi(v)}$$

Highlight results

- Characterization in terms of “reflection positivity”
- Recent extension to the edge model

Algorithmic game theory

Mechanism design

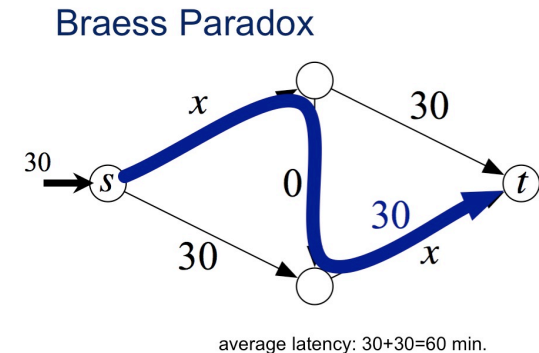
- Socially optimal mechanisms
VCG is optimum for 'public project'

Equilibria in strategic games

- Computation of Nash equilibria
2 players: better approximations
3-players repeated games: hard

- Price of anarchy in network routing

A centralized route guidance does not help to reduce the inefficiency of equilibria in network routing



Algorithmic game theory

Reasoning in strategic games

- Interactive epistemology

Future directions

- Altruistic player behavior
- Smoothed analysis and robustness
- Social networks

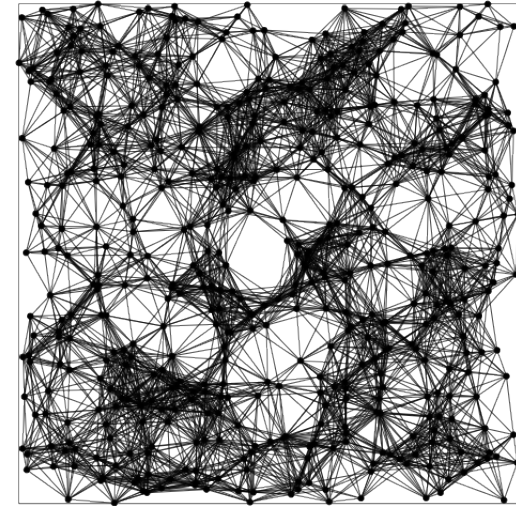
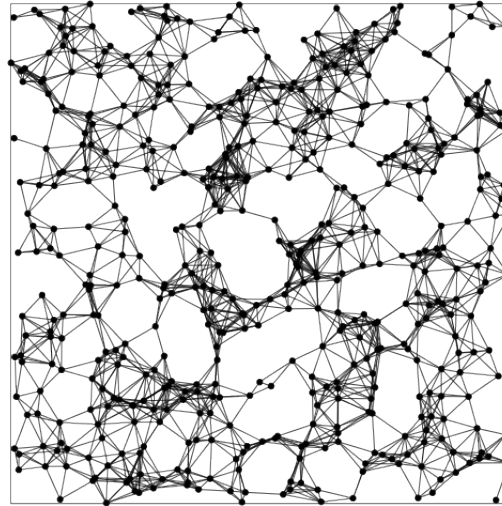
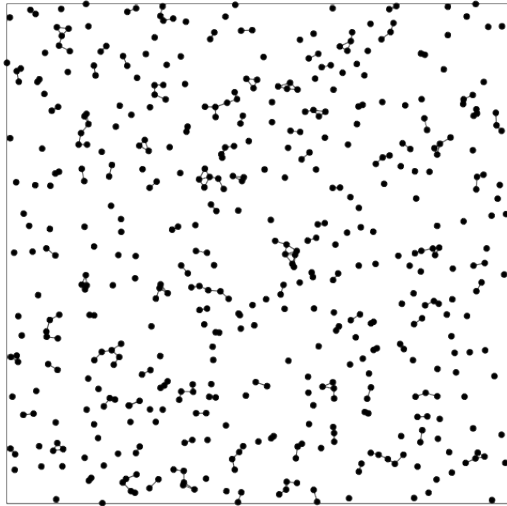
➔ Joint projects with

SEN1 [Software Analysis and Transformation]

SEN3 [Foundations of Software Engineering]

SEN4 [Multi-Agent and Adaptive Computation]

Random geometric graphs



Highlight result

Phase transition behavior for Hamiltonian circuit
and for coloring number

NWO Veni

Cooperation with PNA2

[Probability and Stochastic Networks]

Matroid minors

Is any minor closed matroid property characterized by finitely many forbidden obstructions ?

Can it be tested in polynomial time ?

Highlight result:

Yes, for binary matroids

Challenges:

- Extension to any finite field
- Rota's conjecture:

The class of matroids representable over any given finite field is characterized by finitely many forbidden minors

Societal relevance

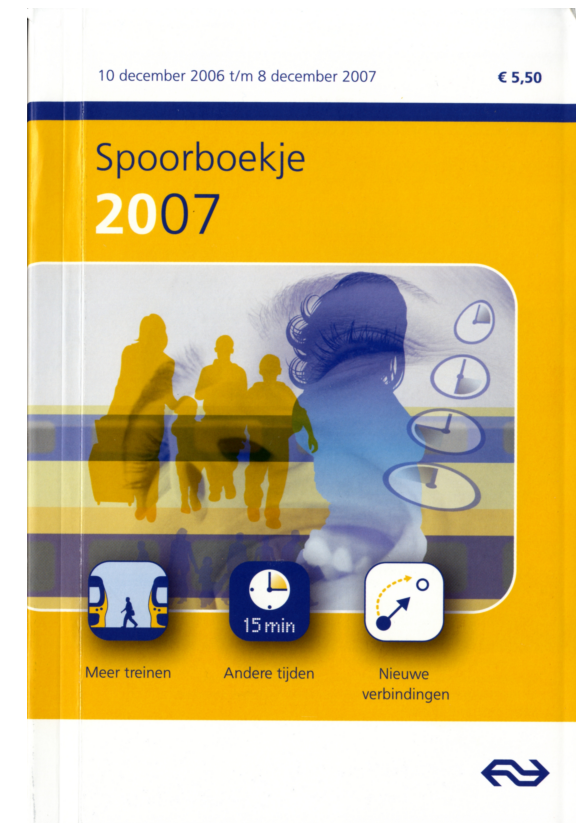
- “The New Dutch Timetable: The O.R. Revolution”
[INFORMS Edelman Award 2008]
- Scheduling internships for medical students



Spin-off



- Optimizing bidding strategies for Google AdWords
(planned, with WatchWord)
- Health care logistics (ambulance planning), planned cooperation with **PNA2** [Probability and Stochastic Networks]



Outreach

- **DisWis:** Educational project about discrete mathematics for high school students [Sigma Prize 2008]
- Internships for high school students at CWI
- Popularization lectures
- Participation in the organization of the International Mathematical Olympiad, Amsterdam 2011

Outreach

Knowledge dissemination: organization of

- 15 international workshops and conferences
- 10 doctoral schools

[Oberwolfach, IPAM, HIM]

Incubator for talent:

- SIAG/Optimization Prize for Vallentin
- Vidi grant for Vallentin
- Veni grant for Mueller
- Rubicon grant for Oliveira
- Tucker Prize finalist: Gijswijt
- Philips Prize for van Leeuwen
- ICALP Best Student paper award for Wojtczak
- Microsoft Research Beyond Search Award for Immorlica and Markakis (with SEN4)

Academic reputation

- **Academia Europaea** Apt, Schrijver
- **Honorary professorship** Waterloo Gerards
- Royal Dutch Academy of Sciences and two German academies; Spinoza and Von Neumann Awards; honorary doctorates Waterloo & Budapest Schrijver
- **Editorships** in leading scientific journals
(SIAM, MOR, MP, Combinatorica, JCTB, TOCL, TPLP, J Logic & Computation, EPTCS,...)
- **Program & Scientific committees**
(MOS, EATCS, MFO, ESF Games, 5ECM, IPAM, TARK, NWO, DIAMANT, LNMB,...)

Q-P-R-V

Quality: awards, academies, honorary degrees, invited lectures (ICM), editorships, grants, publications in top journals (J.AMS, J.EMS, FOCM, GAFA, JCTB, SIOPT, MP)

Productivity: 107 journal & 73 conference articles, 2 books, 2 edited books, 15 book chapters, 10 PhD's

Relevance: for mathematics, computer science, physics, economics, and society

Viability: new areas (algorithmic game theory, algebraic optimization, graph limits); recent staff rejuvenation; worldwide collaboration

SWOT

- S:** Strong group with national and international visibility, and a broad expertise

- WT:**
 - General focus on short term research
 - Limited NWO financing PhD/postdocs
 - Difficulty to recruit talented staff (in NL)

- O:**
 - Increased focus worldwide on applying fundamental mathematics to combinatorics, algorithms and optimization
 - Momentum in algorithmic game theory, with high potential for challenging applications